

Unlocking the power of big data: The importance of measurement error in machine assisted content analysis

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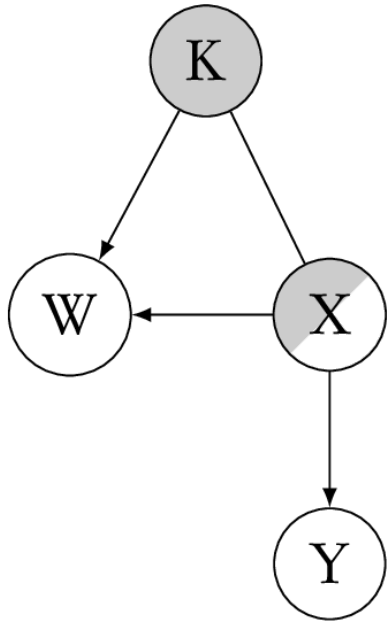
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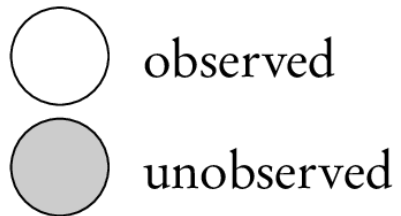
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We can reduce and sometimes even *eliminate* this bias introduced by noise.

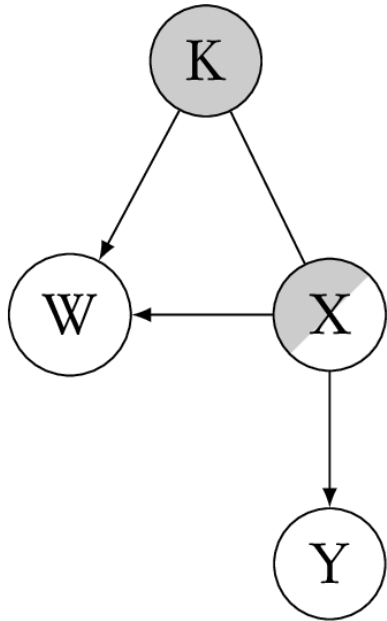
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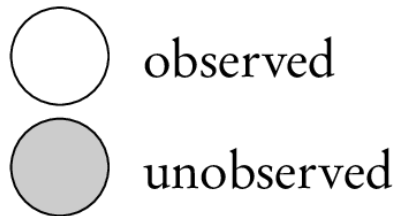


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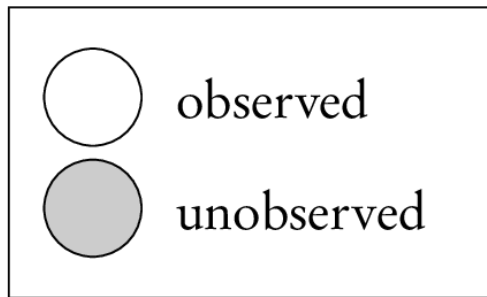
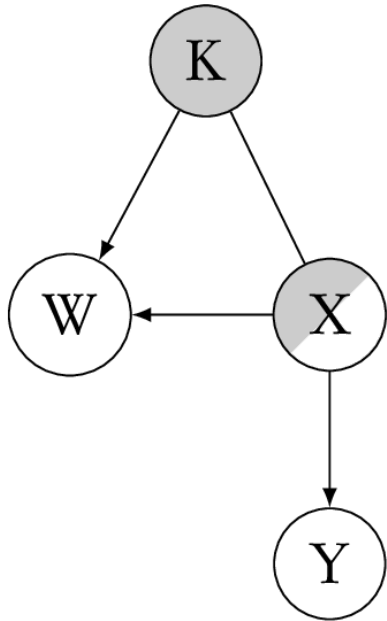


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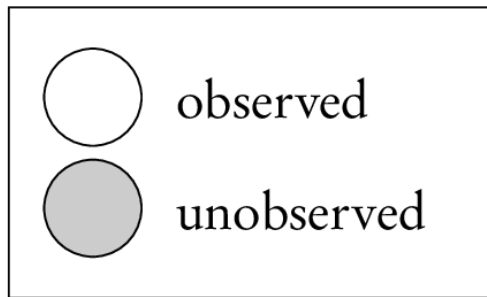
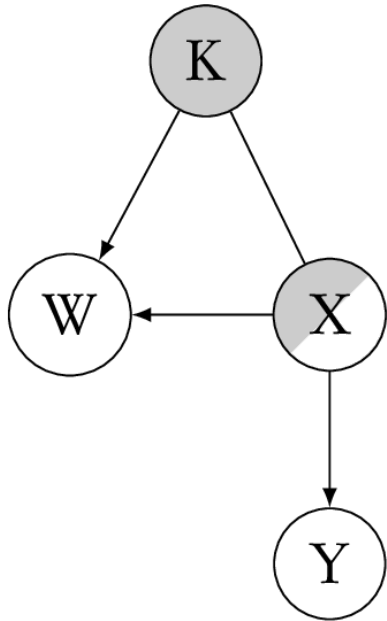


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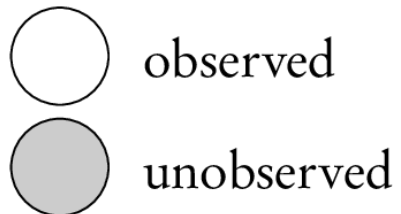
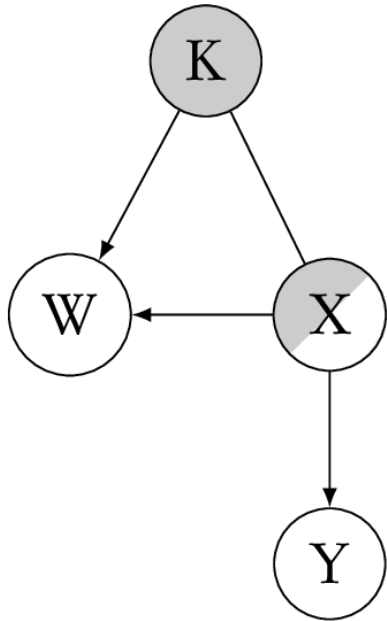
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$x = w + \xi$ because the predictive model makes errors.

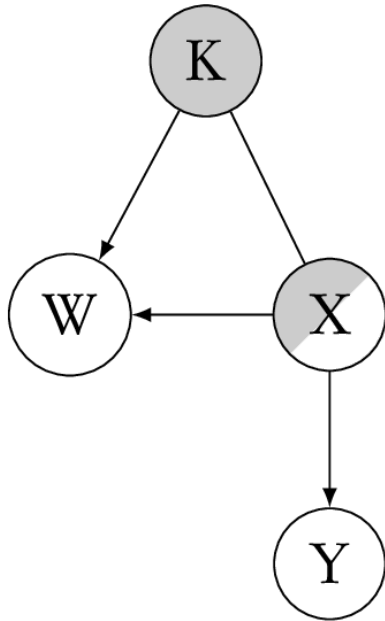
Noise in a *covariate* creates *attenuation bias*.



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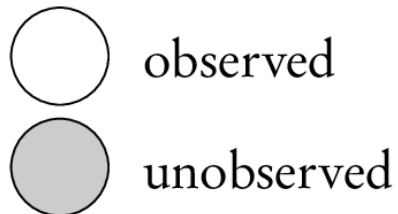
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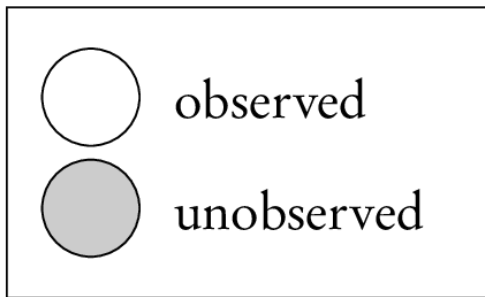
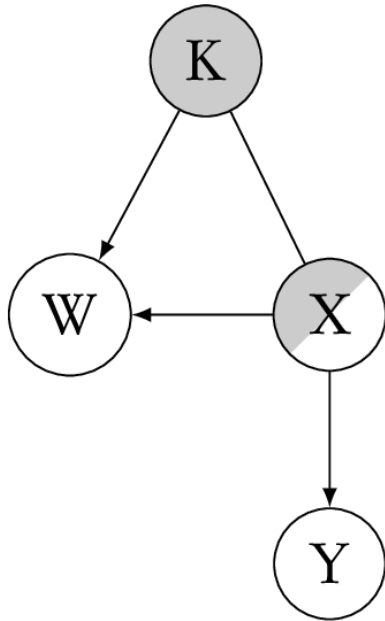
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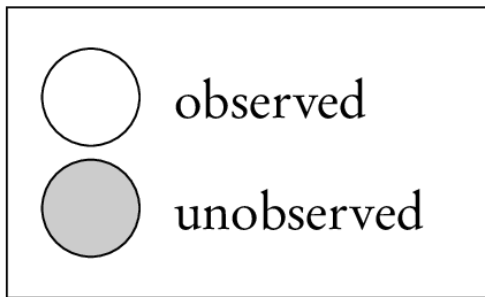
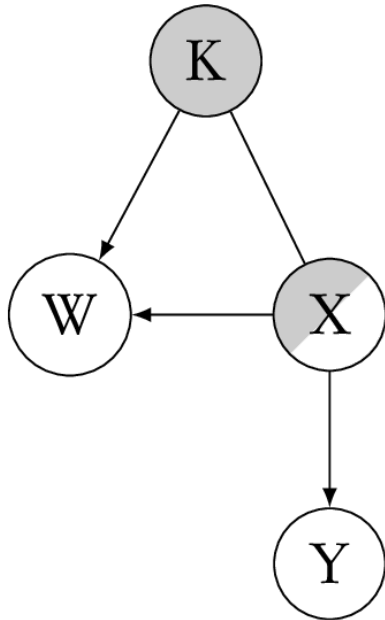
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$$\widehat{B}_w^{\text{ols}} = \frac{\sum_{j=1}^n (x_j + \text{xi}_j - \overline{x + \text{xi}})(y_j - \bar{y})}{\sum_{j=1}^n (x_j + \text{xi}_j - \overline{x + \text{xi}})^2} = \frac{\sum_{j=1}^n (x_j - \bar{x})(y_j - \bar{y})}{\sum_{j=1}^n (x_j + \text{xi}_j - \bar{x})^2}$$

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In this scenario, it's clear that $(\widehat{B}_w^{\text{ols}} < B_x)$.

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- *Bias can be away from 0* in GLMs and nonlinear models or if measurement error is differential.
- *Confounding* if the *predictive model is biased* introducing a correlation the measurement error and the residuals $(E[x_i \varepsilon] = 0)$.

Correcting measurement error

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You can *and should* use it to improve your statistical estimates.

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Disadvantages: Results depend on quality of $\widehat{f(x|w,y)}$; May require more validation data, computationally expensive, statistically inefficient and doesn't seem to benefit much from larger datasets.

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Disadvantages: Limited to OLS models. Requires an unbiased predictor $g(k)$. R support (`meCOR` R package) is pretty new.

2SLS+GMM is designed for this specific problem

PA

Machine Learning Predictions as Regression Covariates

Christian Fong¹ and Matthew Tyler²

¹Assistant Professor, Department of Political Science, University of Michigan, Ann Arbor, MI, USA. Email: cjfong@umich.edu
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Abstract

In text, images, merged surveys, voter files, and elsewhere, data sets are often missing important covariates, either because they are latent features of observations (such as sentiment in text) or because they are not collected (such as race in voter files). One promising approach for coping with this missing data is to find the true values of the missing covariates for a subset of the observations and then train a machine learning algorithm to predict the values of those covariates for the rest. However, plugging in these predictions without regard for prediction error renders regression analyses biased, inconsistent, and overconfident. We characterize the severity of the problem posed by prediction error, describe a procedure to avoid these inconsistencies under comparatively general assumptions, and demonstrate the performance of our estimators through simulations and a study of hostile political dialogue on the Internet. We provide software implementing our approach.

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Disadvantages: Implementation (`{predictionError}`) is new. API is cumbersome and only supports linear models. Not robust if $(E(w\varepsilon) \neq 0)$. GMM may be unfamiliar to audiences.

Testing attention bias correction

I've run simulations to test these approaches in several scenarios.

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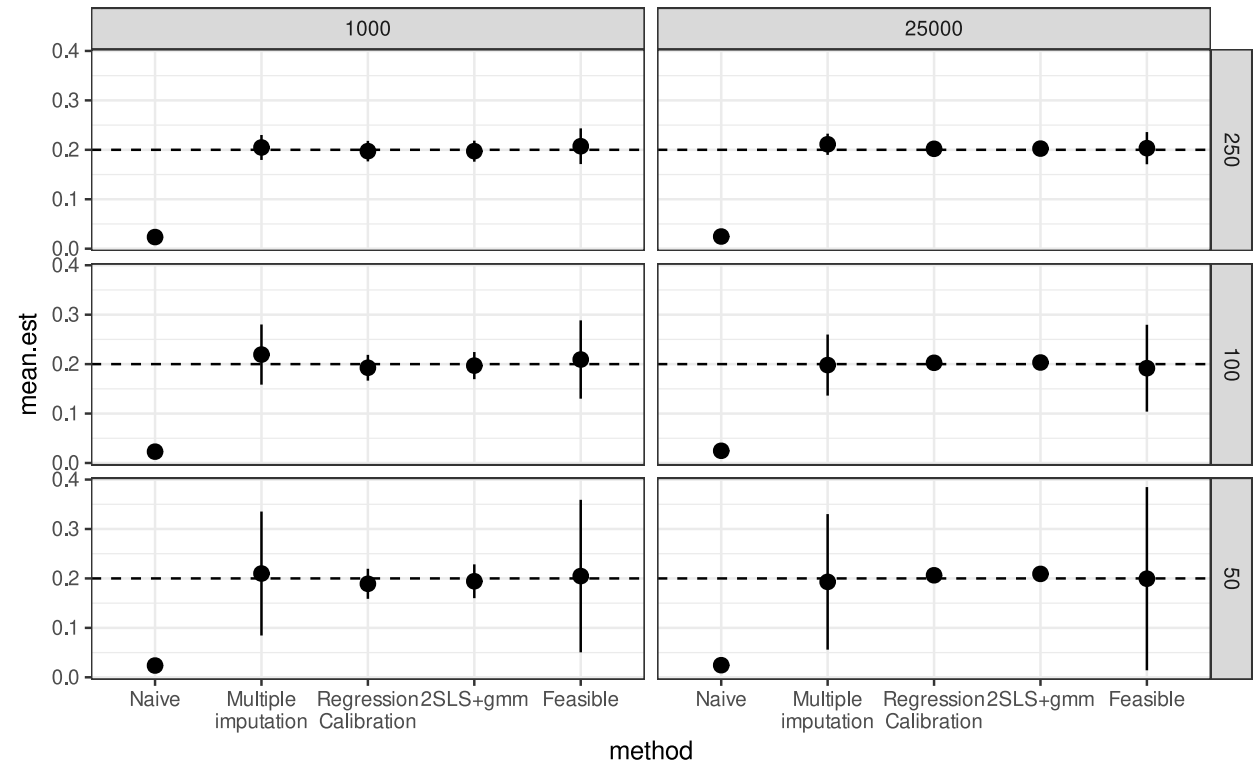
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if w is binary, most methods struggle, but regression calibration and 2SLS+GMM can do okay.

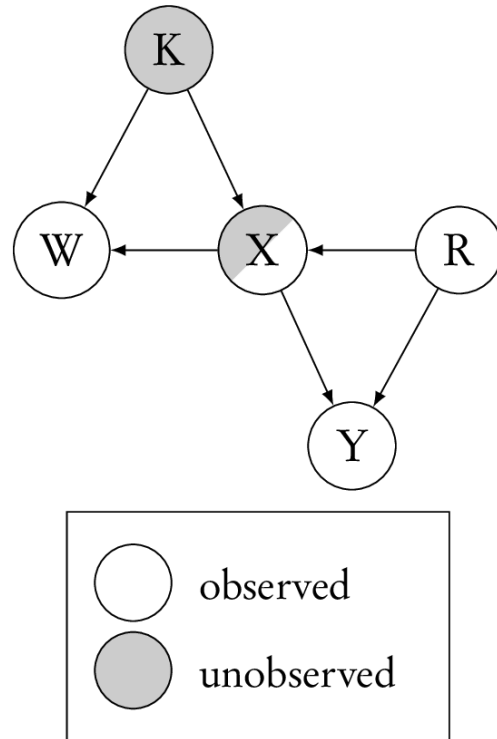
Example 1: estimator of the effect of x

All methods work in this scenario

Multiple imputation is inefficient.



What about bias?



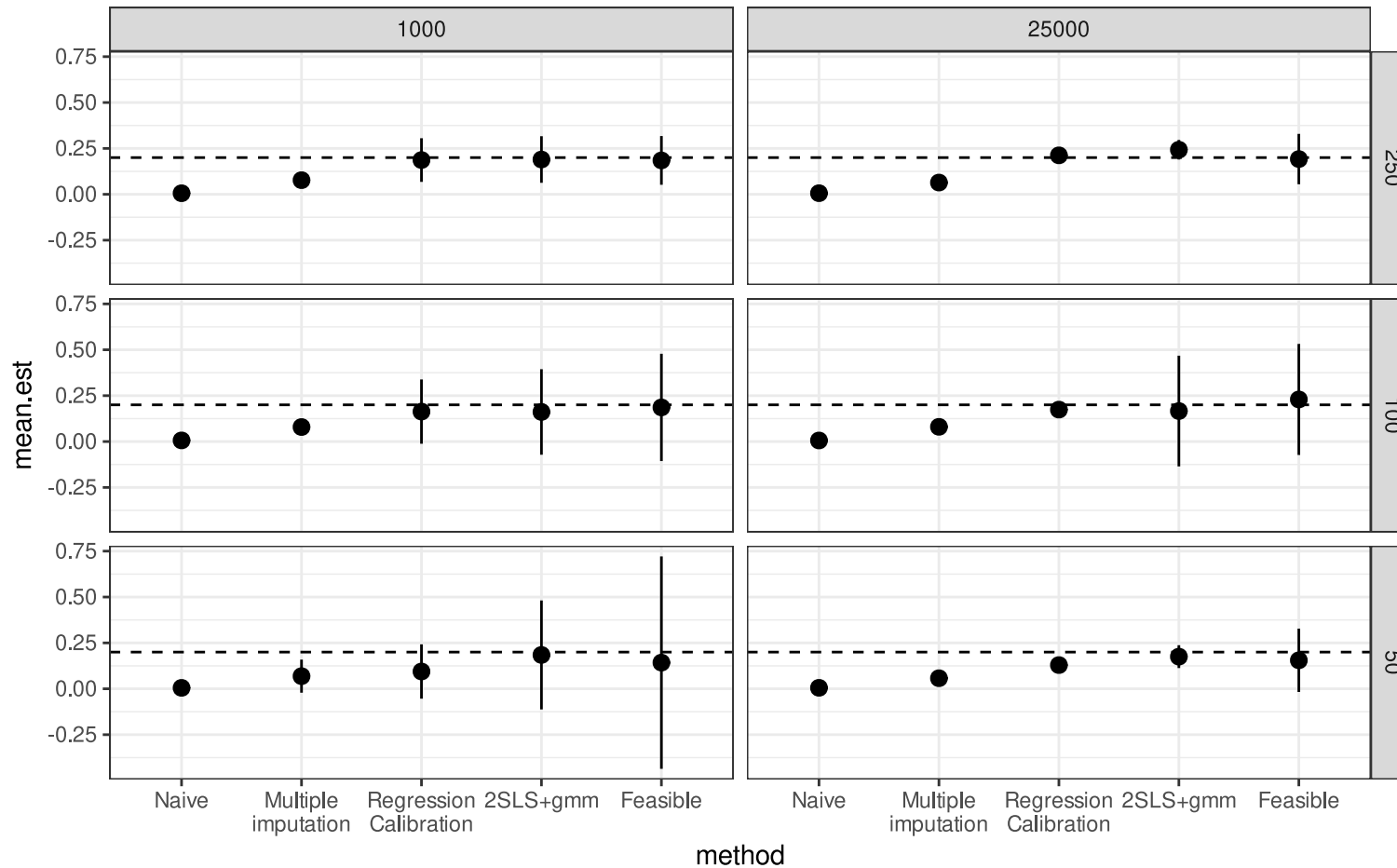
A few notes on this scenario.

$\beta_x = 0.2$, $\beta_g = -0.2$ and $\text{sd}(\epsilon) = 3$. So the signal-to-noise ratio is high.

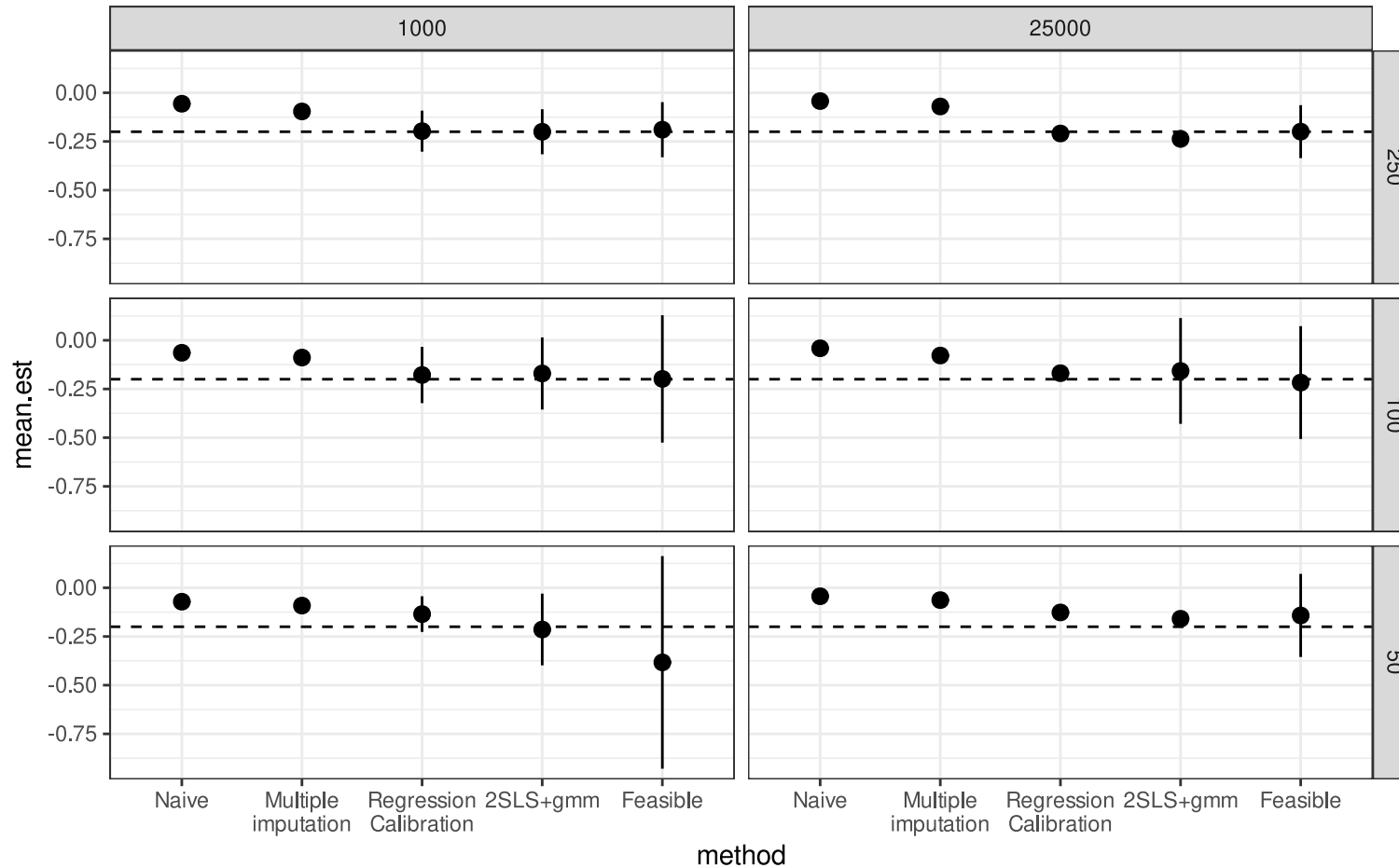
r can be conceived of as a missing feature in the predictive model $g(k)$ that is also correlated with y .

For example r might be the *race* of a commentor, x could be *racial harassment*, y whether the commentor gets banned and k only has textual features but human coders can see user profiles to know r .

Example 2: Estimates of the effect of x



Example 2: Estimates of the effect of r



Takeaways from example 2

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The next scenario has bias that's more tricky.

Takeaways from example 2

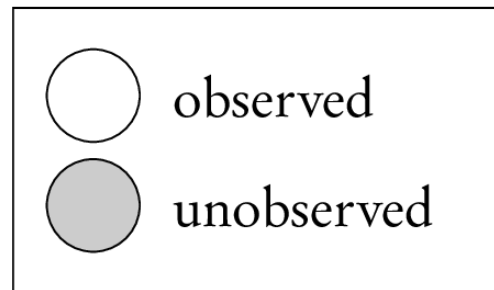
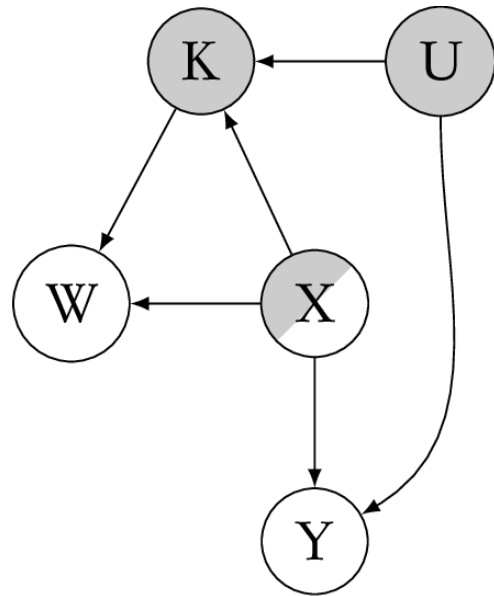
Bias in the predictive model creates bias in hypothesis tests.

Bias can be corrected *in this case*.

The next scenario has bias that's more tricky.

Multiple imputation helps, but doesn't fully correct the bias.

When will GMM+2SLS fail?

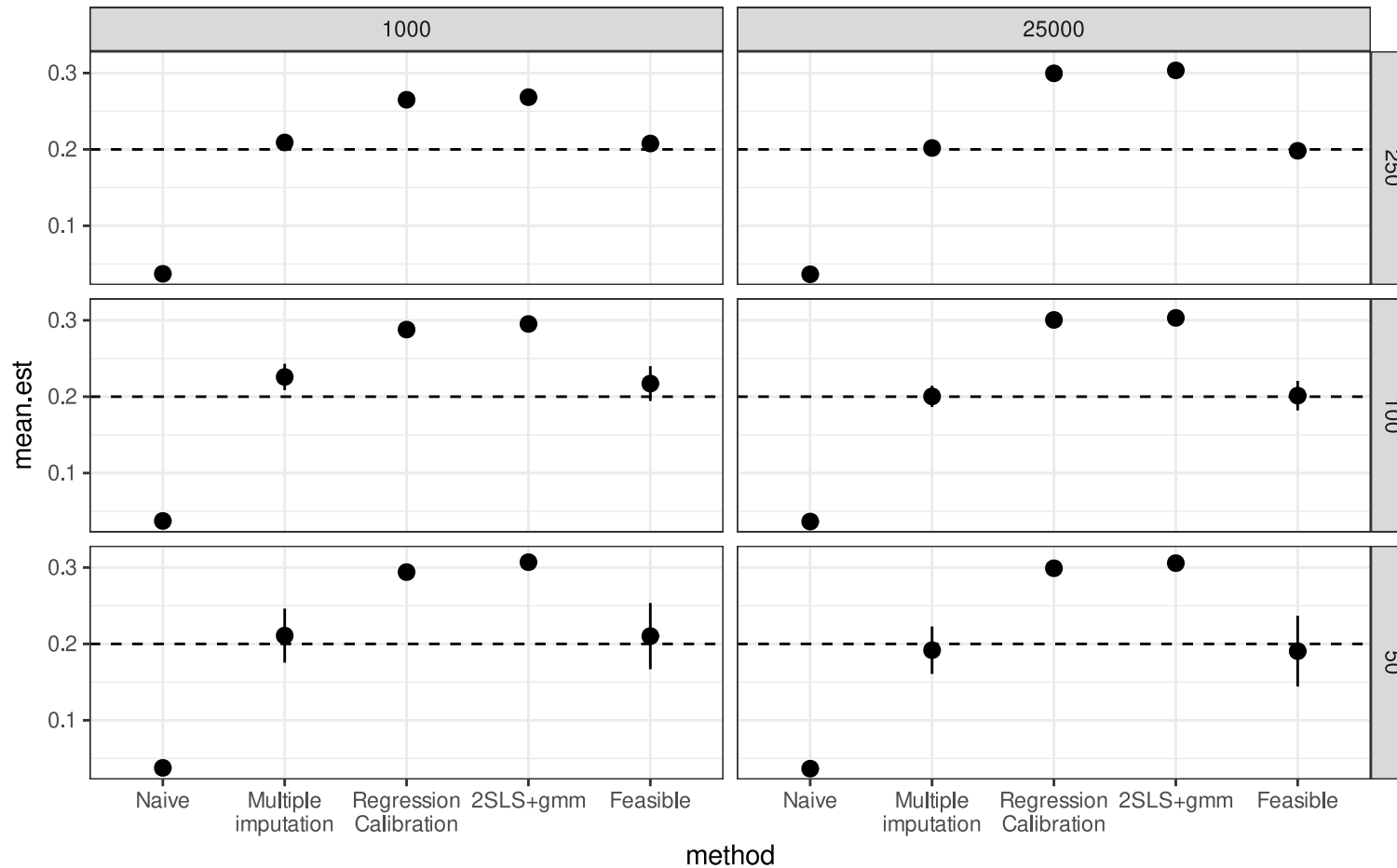


The catch with GMM:

Exclusion restriction: $E[w \varepsilon] = 0$.

The restriction is violated if a variable (U) causes both (K) and (Y) and (X) causes (K) (not visa-versa).

Example 3: Estimates of the effect of x



Takaways

- Attenuation bias can be a big problem with noisy predictors—leading to small and biased estimates.
- For more general hypothesis tests or if the predictor is biased, measurement error can lead to false discovery.
- It's fixable with validation data—you may not need that much and you should already be getting it.
- This means it can be okay poor predictors for hypothesis testing.
- The ecosystem is underdeveloped, but a lot of methods have been researched.
- Take advantage of machine learning + big data and get precise estimates when the signal-to-noise ratio is high!

Future work: Noise in the *outcome*

I've been focusing on noise in *covariates*. What if the predictive algorithm is used to measure the *outcome* $\backslash(y\backslash)$?

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Solving this problem could be an important methodological contribution with a very broad impact.

Questions?

Links to slides:[html](#) [pdf](#)

Link to a messy git repository:

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[@groceryheist](#)

<https://communitydata.science>